

One Qubit

The standard basis for \mathbb{C}^2 is denoted by $|0\rangle_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$, $|1\rangle_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$. The standard basis for $(\mathbb{C}^2)^{\otimes q}$, which has 2^q elements, is denoted by $|0\rangle_q, |1\rangle_q, \dots, |2^q - 1\rangle_q$.

If we pick the standard basis for \mathbb{C}^2 , then a single qubit ($q = 1$) can be represented as $\alpha|0\rangle + \beta|1\rangle = \alpha \begin{pmatrix} 1 \\ 0 \end{pmatrix} + \beta \begin{pmatrix} 0 \\ 1 \end{pmatrix}$ where $\alpha, \beta \in \mathbb{C}$ and $|\alpha|^2 + |\beta|^2 = 1$.

Superposition: $\alpha |0\rangle + \beta |1\rangle$

Complex Amplitudes: α, β

Probabilities: $|\alpha|^2, |\beta|^2$

[An Introduction to Quantum Computing, Without the Physics](#), Giacomo Nannicini, 2017 (2020).